

Warm Up:

Solve for x

$$12 = 2^x$$

3.13 Natural Logarithmic Functions

You invest \$1,000 in a savings account earning 5% APR. How many years will go by before your amount doubles given that it is compounded continuously?

Hide formula

$$2000 = 1000 \cdot e^{.05 \cdot t}$$

$$2 = e^{.05 \cdot t}$$

Hide Answer

$$t = 13.86 \text{ years}$$

Hide Step#1

$$\log_e 2 = \log_e e^{.05 \cdot t}$$

Hide Step#2

$$\frac{\log 2}{\log e} = .05t$$

A savings account compounded continuously doubles in a year. What is the rate?

Assign random values

$$2 = 1e^{r \cdot 1}$$

$$2 = e^r$$

Hide Step#1

$$\log_e 2 = \log_e e^r$$

Hide Step#2

$$\frac{\log 2}{\log e} = r$$

BIG IDEA #1

Notice that the rate is not equal to 100% due to compounding

Big #2

Equations dealing with the value e are very common. To speed the process of solving these equations, a \log_e button was developed on your calculator called Natural log (\ln)

$$\log_e (x) = \ln(x)$$

What are some examples of exponential growth or decay besides interest?

Hide Examples

Population growth

Bacteria

Carbon Dating--half life

E-coli divide every 20 minutes. If you start with 1 single ecoli bacterium how many hours will it take for the ecoli to divide into 1 million ecoli?

FIND r

$$2 = 1e^{r \cdot 20}$$

$$2 = e^{20r}$$

$$\ln 2 = 20r$$

$$r \approx 0.0347$$

Solve for t

$$1000000 = 1e^{0.0347 \cdot t}$$

$$\ln 1000000 = .0347t$$

$$t \approx 398.6 \text{ minutes}$$

$$6.64 \text{ hours}$$